
Statistical Signal Processing Project Report Group-7

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Abstract

1 The project involves the comprehension and implementation of state of the art tech-
2 niques involved in the estimation of direction of source. We ended implementing
3 two state of the art techniques which involves different experimental settings. We
4 will discuss about them in the upcoming sections.

5 1 Direction of arrival estimation using Information Geometry (1)

6 The paper explores the idea of using information geometry as the similarity measure between the
7 observations.

8 1.1 Description of Matlab files

9 There are basically two files. The first file implements the algorithm and plots the spectrum while
10 comparing its with state of the art MUSIC and MVDR algorithms, while the second file implements
11 the Monte Carlo simulation and compares their performance on different SNR values. Following is
12 the description:

13 1.1.1 doa.m

14 The file implements the signal model and IG algorithm, and compares its spatial spectrum with
15 MUSIC and MVDR. MUSIC and MVDR are implemented via in-built phased library functions
16 present in MATLAB.

17 1.1.2 monte_carlo_doa.m

18 The file implements the Monte Carlo simulation for all the three algorithms. The simulation is run
19 for different values of SNR depending upon the problem. Sources are kept to 2 in this file.

20 1.2 Description of Functions and Modules from MATLAB

21 In the paper we had to compare the results of the proposed method IGPencil as against standard
22 methods of source angle estimation MUSIC and MVDR. The implementation of MUSIC and MVDR
23 is already present in the **Phased System Array Toolbox** of MATLAB. Functions used in the setup
24 model are as follows:

- 25 • **phased.ULA** : For modelling a uniform linear array (ULA) containing 11 isotropic antennas
26 spaced 0.5 meters apart.

- 27 • **sensorsig** : For the multichannel signal received by ULA.
- 28 • **phased.MVDREstimator** : Scans an MVDR beam over the specified region
- 29 • **phased.MUSICEstimator** : Scans a MUSIC beam over the specified region

30 1.3 Steps of Execution

31 There have been two major implementations done by us:

- 32 • **IGPencil** : In this method we need to plot the spectrum of

$$f(\phi) = \frac{1}{(\log \mathbf{a}(\phi)^H \hat{\mathbf{R}}_{xx}^{-1} \mathbf{a}(\phi))^2}, \quad \phi \in [-\pi/2, \pi/2] \quad (1)$$

33 and the source angles could be estimated from the maximas of the spectrum.

- 34 • **Monte Carlo** : We have to run the IGPencil, MUSIC and MVDR models for 1000 different
- 35 signals at a particular SNR which has to be varied in a certain range. Then we plotted the
- 36 the graph of MMSE vs SNR (in dB) for measuring the statistical performance.

37 The application of algorithm can be broken down in following steps

- 38 1. Create a uniform linear array model of 11 elements placed at separation of $\lambda/2$ with equal
- 39 power of unity. Allocate sources to the desired directions and generate 100 instances of
- 40 signal at each element with desired level of White Gaussian Noise.
- 41 2. Proceed to calculate the energy covariance matrix $\hat{\mathbf{R}}_{xx}$ which is just equal to $\mathit{signal} * \mathit{signal}^H$. This would serve the purpose of true covariance matrix.
- 42
- 43 3. For an angle span of $[-90^\circ, 90^\circ]$, calculate the IG Pencil function 1 for each degree.
- 44 4. Maximas of the above function will give you the direction of the sources.
- 45 5. Normalize the function and calculate the spatial spectrum, in decibels.
- 46 6. Compare it with algorithms, MUSIC and MVDR (implemented using in-built functions) by
- 47 plotting the spatial spectrum.

48 The Monte Carlo simulation and comparisons can be done in following manner.

- 49 1. Create 20 divisions for the range of SNR you want to evaluate. For each chosen SNR in the
- 50 range, generate 100 samples (Monte Carlo samples) of signal. Sources are limited to two in
- 51 these simulations
- 52 2. Implement all three algorithms and calculate parameters such as estimated angle, variance,
- 53 root mean squared error for each SNR value for each source.
- 54 3. Plot the root mean squared error curve and the estimated angle for each algorithm for each
- 55 source.

56 1.4 Experimental Setup

57 Set up a uniform linear antenna array of 11 elements spaced $0.5 \lambda/2$ metres apart. For the first

58 experiment SNR is kept at 10dB and the sample size at each antenna is kept at 100. For Monte Carlo

59 simulations, at each SNR, 100 samples of signal model is generated. We'll run the code for 4 setups

60 with varying number of sources and varying the values of SNR as well.

- 61 1. Generate a set of 10 sources with equal unitary power and uniform separation in degrees
- 62 from range $[-60^\circ 60^\circ]$ buried under white noise of SNR 10dB and a set of $K = 100$ time
- 63 snapshots have to be considered.
- 64 2. Take two sources at angles $[-20^\circ 30^\circ]$ where the noise is varied for the sources. For
- 65 simulations we conduct 1000 Monte Carlo experiments with SNR from range -20dB to
- 66 20dB.
- 67 3. Take two sources at angles $[-20^\circ 25^\circ]$ where the noise is varied for the sources. For
- 68 simulations we conduct 100 Monte Carlo experiments with SNR from range -5dB to 40dB.

69 4. Lastly take 13 sources with equal unitary power and uniform separation in degrees from
70 range $[-60^\circ 60^\circ]$ buried under white noise of SNR 10dB and a set of $K = 100$ time snapshots
71 have to be considered.

72 1.5 Results

73 Performing the first experiment in which 10 sources were located at equidistant from each other with
74 in the range of $[-60^\circ 60^\circ]$, we compared the spatial spectrum of all the three algorithms, IG, MUSIC,
75 and MVDR as shown in Figure 1. It was found out that the performance of IG method was at par or
similar to MUSIC and MVDR methods.

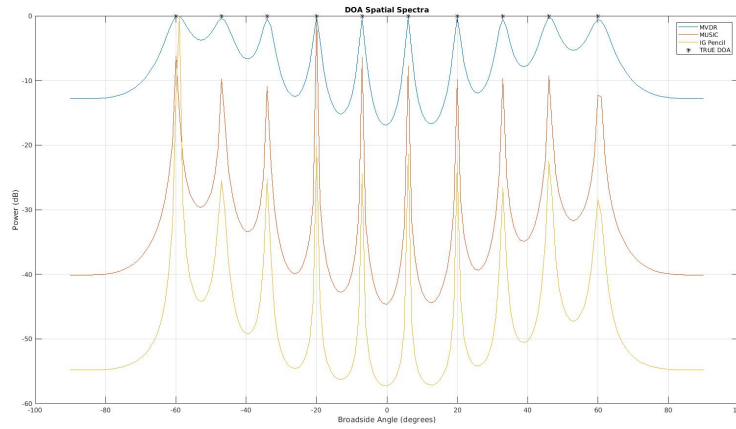


Figure 1: Spatial Spectrum Comparison of IG with MUSIC and MVDR when 10 sources are kept equidistant from $[-60^\circ, 60^\circ]$

76

77 To investigate further, we ran Monte Carlo simulations for two sources kept far apart at $\theta =$
 78 $(-20^\circ, 30^\circ)$. The SNR for this experiment was varied between $[-20, 20]$ dB. To measure the perfor-
 79 mances, we plotted the mean square root error v/s SNR as shown in Figure 2. It can be seen that as
 80 we increase the SNR, performance of IG exactly follows the MVDR and also, at lower levels it is
 81 comparable to MUSIC, and MVDR.

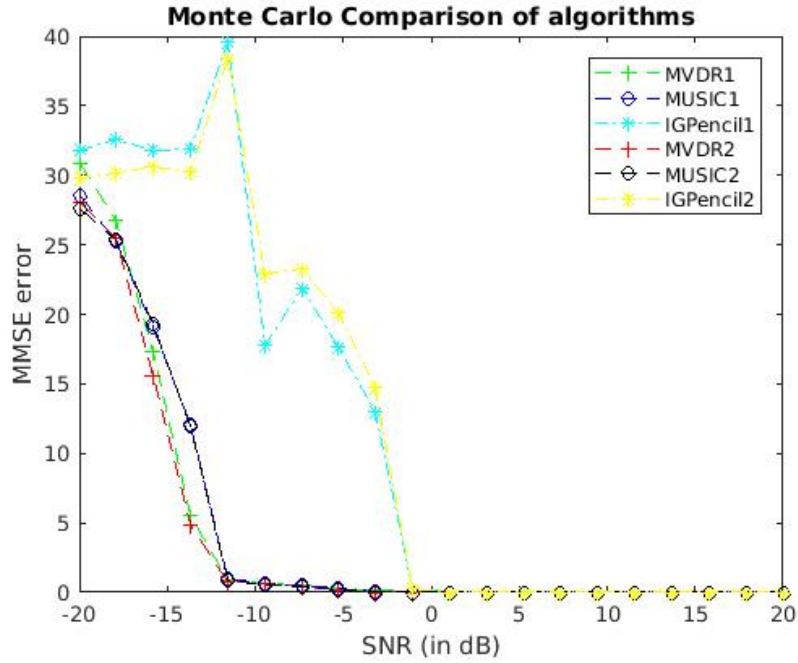


Figure 2: Root Mean square error comparison of Monte Carlo simulation of IG with MUSIC and MVDR at different SNRs in range $(-20, 20)$ dB when 2 sources are kept far apart at $(-20^\circ, 30^\circ)$

82 But, when sources are placed closer at $\theta = (-20^\circ, -25^\circ)$, and compare the performances for SNR
 83 range $(-5, 40)$ dB as shown in Figure 3, we found that the error for IG method performed much
 84 better than MUSIC, or MVDR especially at lower SNR values. Comparing the error graphs of all
 85 three methods in th figures 4, 5 and 6, the argument that IG provided the better resolution at lower
 86 SNR values is strengthened.

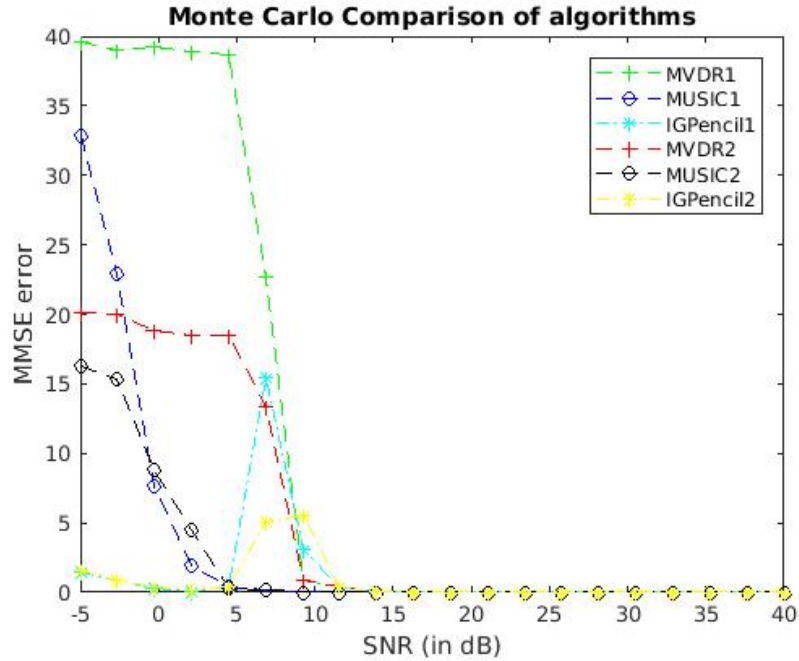


Figure 3: Root Mean square error comparison of Monte Carlo simulation of IG with MUSIC and MVDR at different SNRs in range $(-5, 40)$ dB when 2 sources are kept close at $(-25^\circ, 20^\circ)$

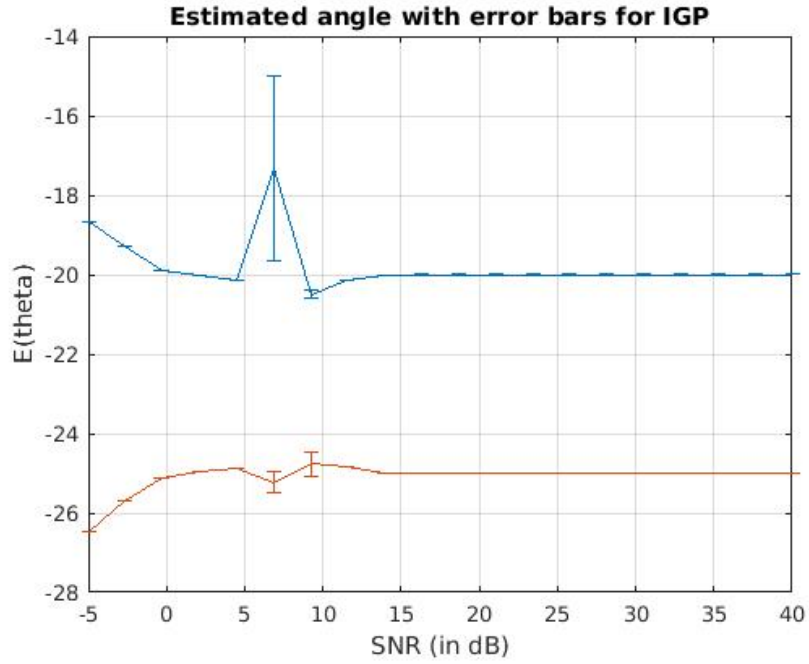


Figure 4: Error graph: IG pencil method

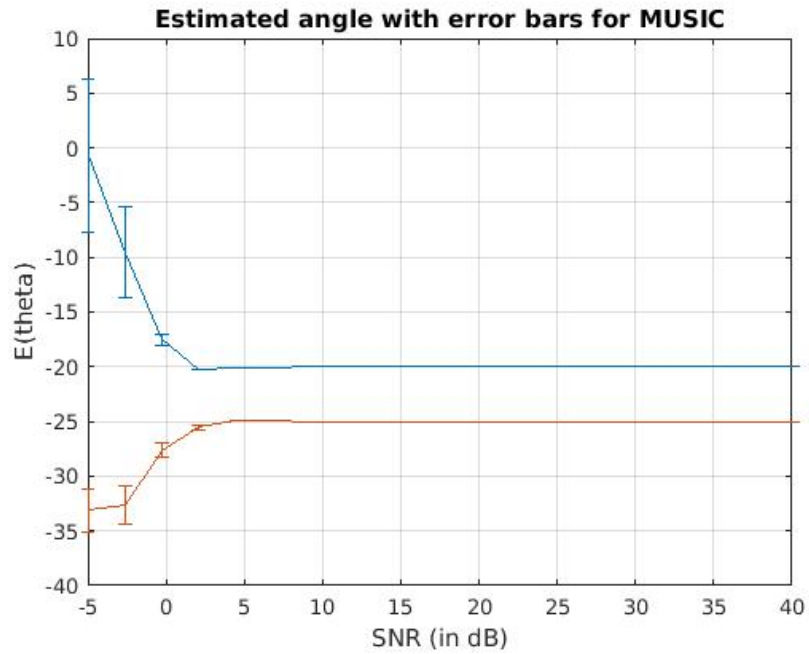


Figure 5: Error graph: MUSIC

87 Finally, we increased the number of sources distributed to 13, taken at SNR of 10 dB. MVDR and
 88 MUSIC even failed to recognize more than 8 sources. But, IG method identified all the sources and
 89 located them correctly. It can be seen from spatial Spectrum plots in Figure 7

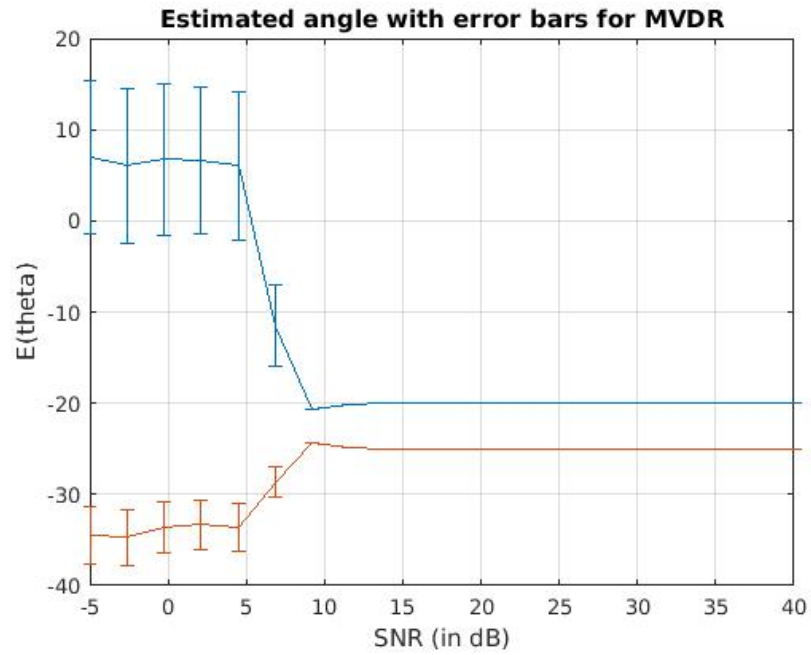


Figure 6: Error graph: MVDR

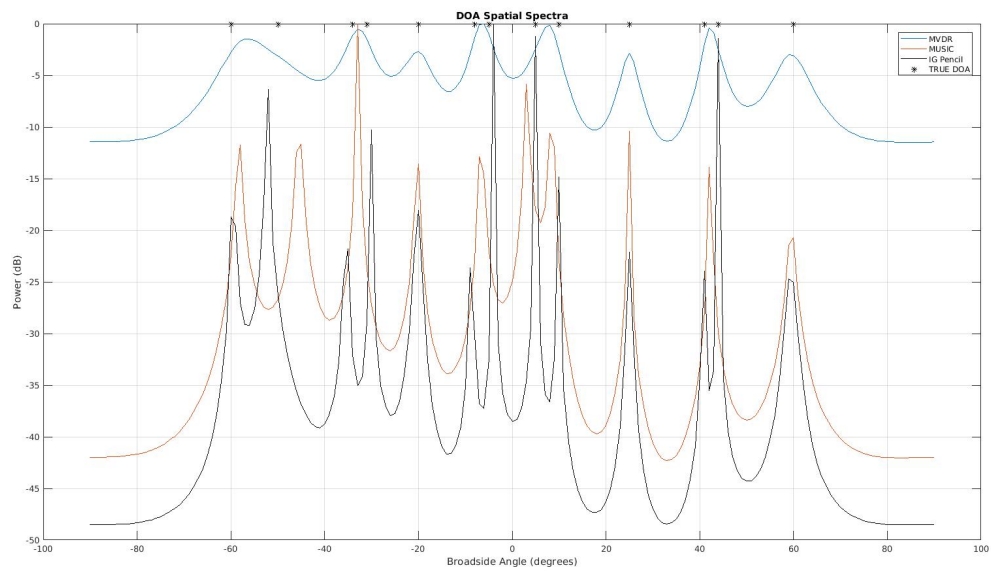


Figure 7: Spatial Spectrum Comparison of IG with MUSIC and MVDR when 13 sources are kept in $[-60^\circ, 60^\circ]$

90 **1.6 Report from MATLAB**

91 Published report from MATLAB is attached at last.

92 **2 Source tracking using moving microphone arrays for robot audition (2)**

93 **2.1 Description of MATLAB files and functions**

94 The following files were used while implementing the algorithm:

95 **2.1.1 calc_distance.m**

96 Function that takes two matrices as input and returns the maximum of the absolute value of the
97 difference between the two.

98 **2.1.2 complex_gauss.m**

99 Function that takes point and covariance matrix (as a complex number) as input and returns the
100 probability of the point from the circular Gaussian distribution with zero mean and given covariance
101 matrix.

102 **2.1.3 SSP_EM.m**

103 This file runs the subroutine EM algorithm for at max 50 iterations. It uses certain threshold for the
104 convergence. This file assumes following input from file **sampler.m**[2.1.4]

- 105 • microphone position
- 106 • J sampled state (x, y, v_x, v_y) of particles.(size = $4 \times J$)
- 107 • STFT of the signal recieved by microphones.(size = $2 \times K$; K = no. of frequency bins.)
- 108 • ϵ to calculate the $\Gamma(t, k)$ for each instant t and each frequency bin k .

109 This subroutine returns probability vector which inturn is used to update weights $w_j^{(t)}$. This subroutine
110 calls complex_gauss and calc_distance as helper functions.

111 **2.1.4 sampler.m**

112 This is the main script for the second paper's implementation. It defines the 3 parts of the algorithm,
113 source motion, sampling possible source positions and updating the weights for the sampled source
114 position using SSP_EM function on the convolution of the RIR and STFT of the observed speech
115 signal. Then it plots the KDE contour plots for each time step.

116 **2.1.5 stft.m (3)**

117 Function takes in the time domain signal values, sampling rate, window, and hop length(here it is the
118 same as window length) and outputs the STFT of the given signal. This function has been ported
119 from MATLAB File Exchange.

120 **2.1.6 RIR (4)**

121 Function has been ported from the RIR library. It computes the RIR for given source-microphone
122 geometries when the reverberation time and room dimensions have been supplied.

123 **2.2 mvnpdf**

124 Function generates the given number of samples from a multivariate normal distribution with given
125 mean and covariance matrix.

126 **2.3 ksdensity**

127 Calculates the probability density for given set of sampled points and their corresponding weights
128 over a given region using the Kernel Density Estimator. Gives probability density values for the pdf

129 approximated as

$$p(\mathbf{s}(t)|\mathbf{Z}_{1:t}, \phi_y(t, k), \phi_R(t, k)) \approx \sum_{j=1}^J \tilde{w}^{(j)}(t) \delta_{\mathbf{s}^{(j)}(t)}(\mathbf{s}(t)), \quad (15)$$

130 2.4 Steps of Execution

- 131 • We generate the microphone positions from its initial and final positions and the source
132 model according to the given equation for a Langevin Model.

$$\mathbf{s}(t) = \mathbf{F}(t)\mathbf{s}(t-1) + \mathbf{u}(t), \mathbf{u}(t) \sim \mathcal{N}(0_{4 \times 1}, \mathbf{Q}(t)) \quad (2)$$

133 The initial positions for the actual source and the sampled source positions are randomly
134 assigned inside the room and a 2s signal from the TIMIT database.

- 135 • For each time step the following actions are taken –
 - 136 – The new true source position is sampled from the source model.
 - 137 – STFT of the part of signal observed in this time step is generated and convolved with
138 the RIR generated for the current source-microphone positions.
 - 139 – For each frame of the STFT, we sample the J possible source positions according to
140 the source motion model. Then for this J -long set of sampled positions, we calculate
141 the weights to approximate the source position distribution using SSP_EM function.
142 Note: We also remove the zero valued frequency components from STFT
 - 143 – We plot the kernel density contours for the current sampled source positions using the
144 ksdensity function.

145 2.4.1 EM

146 The file assumes some information like speed of sound and sampling frequency, and calculates Γ and
147 \mathbf{h} . For calculating Γ the diagonal loading factor is taken to be $\epsilon = 0.1$. It then finds $\phi_{R,j}(t, k)$ and
148 $\phi_{y,j}(t, k)$ and $\Phi_j(t, k)$ for each of the j and k . Using $\Phi_j(t, k)$ it goes to while loop and finds μ and
149 ψ using μ alternately, until convergence. The equations for both of them is given as-

$$\mu^{(\ell-1)}(t, k, j) \triangleq \mathbb{E}[x(t, k, \theta_j)|z(t, k), \theta^{(\ell-1)}] = \frac{\psi_j^{(\ell-1)} \mathcal{N}^c(z(t, k)|0_{2 \times 1}, \Phi_j(t, k))}{\sum_{j=1}^J \psi_j^{(\ell-1)} \mathcal{N}^c(z(t, k)|0_{2 \times 1}, \Phi_j(t, k))}$$

150 and

$$\psi_j^{(\ell)} = \frac{1}{K} \sum_{k=1}^K \mu^{(\ell-1)}(t, k, j)$$

151 Finally after convergence it finds the probabilities $p(\mathbf{Z}_t|\theta_t^{(j)})$ that are returned.

152 2.5 Experimental Setup

- 153 • Source, microphone and room params : Experimental setup consist of a $6m \times 6m \times 3.5m$
154 dimensional room. The source state is modelled by Langevin motion model. Source position
155 is observed after every 0.375s. The 2 microphone start form $([1.35,1,1.5]; [1.65,1,1.5])$ and
156 are moving in a straight line upto position $([4.85,1,1.5]; [5.15,1,1.5])$ for 10s. The initial
157 positions for the source is selected randomly uniformly from a region which is 1.5m away
158 from each of the walls. The source motion model params are $\bar{v} = 1m/s$ and $\beta = 2$.
- 159 • Signal : 10s signal generated from TIMIT database by joining 3 signals and clipping it
160 till 10s. However, we analyse only the first 2s of this signal to reduce the time taken for
161 computation. $f_s = 8kHz$ for the 10s sound signal. For the signals of the timit database,
162 sampling is done at 16kHz, so we downsample these signals.
- 163 • RIR params : Speed of sound taken as $c = 340$ and the reverberation time is 0.5s
- 164 • The number of sampled source positions are $J = 100$ which has been reduced from that
165 mentioned in the paper to reduce computation time. The initialisation for these J points is
166 similar to the initialisation of the true source. We do not ignore the sampled points which lie

167 outside the room but count their number and check their value at the end to see how valid
168 our assumption was. The model for sampling was same as the source motion model but
169 the interval between 2 samplings is now the frame length so the Q and F matrices were
170 changed accordingly to accomodate this.

- 171 • STFT params : We set the number of points for STFT as 512 and rectangular window with
172 frame length 50ms. We take a hop equal to frame length, thus preventing overlap.
- 173 • We remove all frequency components which have 0 contribution from the STFT as these
174 result in singularities when using the SSP_EM procedure.
- 175 • ksdensity is calculated only for the region of the room for 61 points along each axis.

176 .

177 For EM no extra parameter was required, all the required parameters were known from sampler file.
178 The ψ vector of length J was initialized by constant vector of $1/J$, Using this vector the alternating
179 optimization scheme was initialized. The only assumption taken was to calculate $w^{(j)}(t) = w^{(j)}(t -$
180 $1)\psi_j^{(L)}\mathcal{N}^c(\mathbf{z}(t, k)|0_{2 \times 1}, \Phi_j(t, k))$ as $w^{(j)}(t) = w^{(j)}(t-1)\psi_j^{(L)} \max_k(\mathcal{N}^c(\mathbf{z}(t, k)|0_{2 \times 1}, \Phi_j(t, k)))$.
181 We should have taken $w^{(j)}(t) = w^{(j)}(t-1)\psi_j^{(L)} \prod_k \mathcal{N}^c(\mathbf{z}(t, k)|0_{2 \times 1}, \Phi_j(t, k))$ but it was giving
182 infinite values of weights. The convergence criterion is either 50 iterations of EM or either the
183 maximum absolute difference between the elements of μ is less than 0.0001.

184 2.6 Results

185 The results differ a bit from the actual plots which can be because we have scaled down the problem
186 to the level that it has become difficult to obtain convergence. The reductions in maxiter for EM
187 algorithm and the length of the sound signal and the number of particles were done to get a reasonable
188 computation time on a laptop. Thus, we might not have achieved optimum convergence conditions.
189 Our code takes approximately 60 minutes for running.

190 Also, the number of points which lie outside the room among the true source positions and the
191 sampled source positions are and which shows that some sort of truncation needs to be applied on the
192 sampling procedure. We propose that the paper should have used a truncated gaussian (truncated to
193 be always inside the room).

194 In the EM procedure, we take the maximum of the probability of the K components and not their
195 multiplication as it leads to very large values many being Inf, which makes kernel density estimation
196 impossible . One workaround for this can be clipping the probability density values to some large
197 number but even then, the KDE performance would differ from optimal.

198 We thus believe that there were many important implementational details not mentioned in the paper
199 and for these we had to make appropriate assumptions to get valid results. Some of these assumptions
200 might be different from that made by the authors. Finally, the computational capacity used by the
201 authors might be very large of which there is no mention in the paper . Published file from MATLAB
202 is attached in the end.

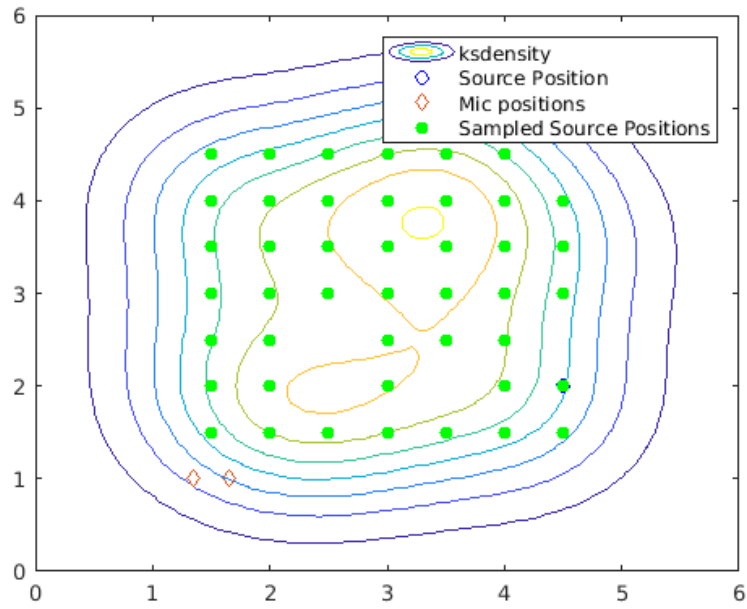


Figure 8: distribution of particles at $t=0$ sec

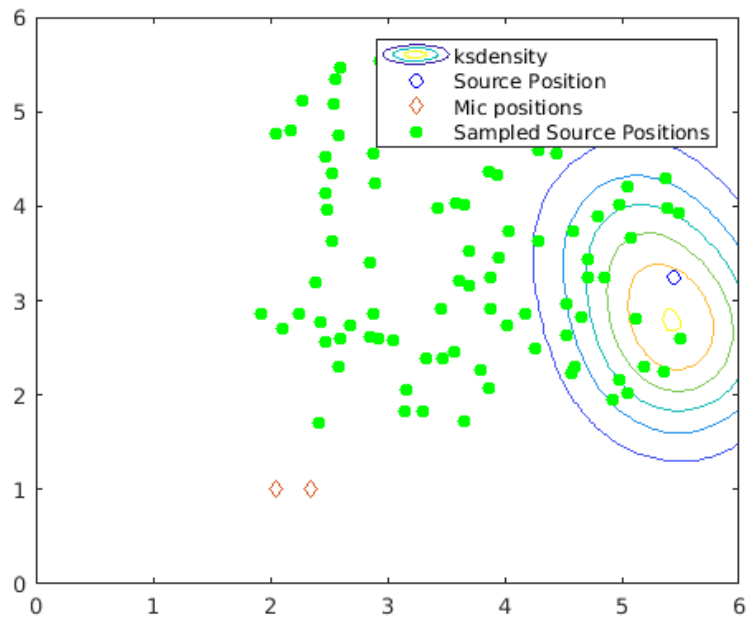


Figure 9: distribution of particles at $t=0.375$ sec

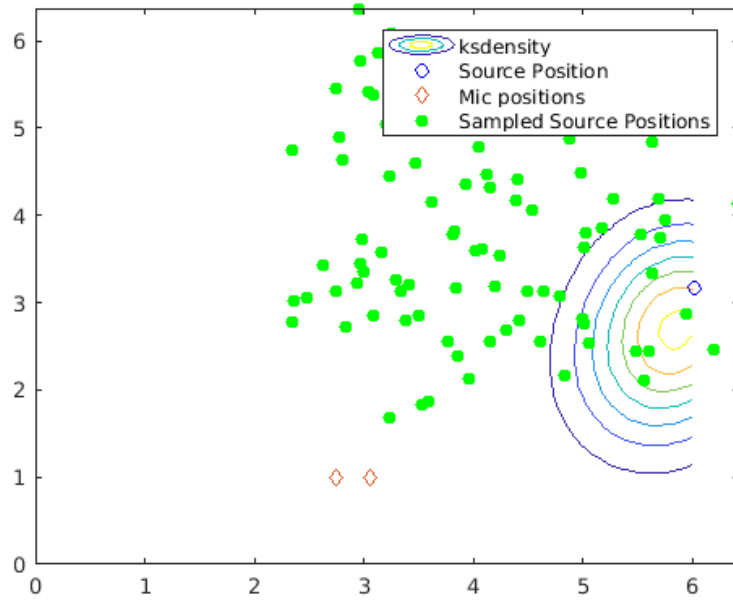


Figure 10: distribution of particles at $t=0.75\text{sec}$

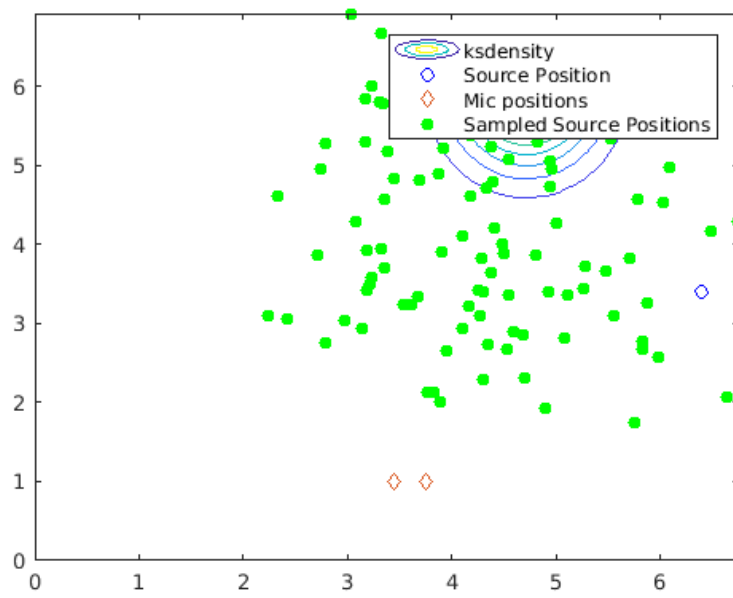


Figure 11: distribution of particles at $t=1.125\text{ sec}$

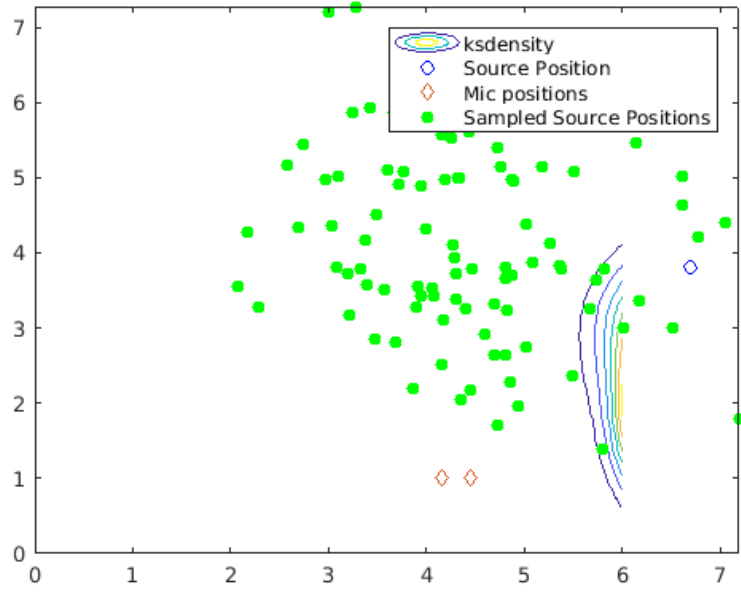


Figure 12: distribution of particles at t=1.5 sec

203 **References**

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